

1 Constant Acceleration by Separation of Variables

- (a) **Calculate:** Treat Newton's 2nd law as a separable differential equation and solve for the velocity and position as a function of time of an object that is all of the following:
- moving in one dimension,
 - not initially at the origin of coordinates,
 - moving with a non-zero initial speed,
 - experiences a constant force.
- (b) **Reflect:** Do your answers look familiar? If yes, from where? If not, how would you have to modify these equations to be similar to equations you know?

2 Separable ODE linear + constant

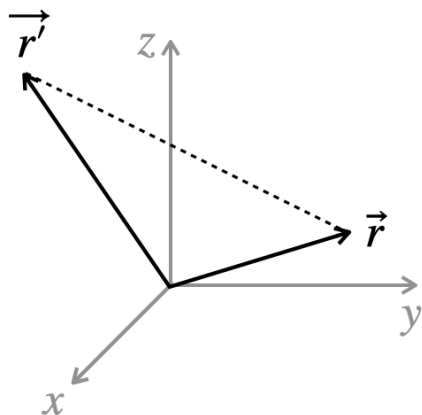
Solve the differential equation:

$$\frac{dv}{dt} = -b - cv \text{ where } v(t=0) = v_0$$

3 Distance Formula in Curvilinear Coordinates

The distance $|\vec{r} - \vec{r}'|$ between the point $\vec{r}$ and the point $\vec{r}'$ is a coordinate-independent, physical and geometric quantity. But, in practice, you will need to know how to express this quantity in different coordinate systems.

- (a) Find the distance $|\vec{r} - \vec{r}'|$ between the point $\vec{r}$ and the point $\vec{r}'$ in rectangular coordinates.



- (b) Show that this same distance written in cylindrical coordinates is:

$$|\vec{r} - \vec{r}'| = \sqrt{s^2 + s'^2 - 2ss' \cos(\phi - \phi') + (z - z')^2}$$

Hint: You may want to use the textbook: GMM: Change of Coordinates

(c) Show that this same distance written in spherical coordinates is:

$$|\vec{r} - \vec{r}'| = \sqrt{r'^2 + r^2 - 2rr'[\sin\theta\sin\theta'\cos(\phi - \phi') + \cos\theta\cos\theta']}$$

Hint: You may want to use the textbook: GMM: Change of Coordinates

(d) Now assume that $\vec{r}'$ and $\vec{r}$ are in the x - y plane. Simplify the previous two formulas.